

IN THE CLAIMS:

Following is the listing of pending claims in the present application.

1(Original). A method of determining error magnitudes in Reed-Solomon decoding, wherein a vector of v syndromes E_i and v error locations l_j are determined from a received codeword, and error magnitudes e_{l_j} at the v error locations can be determined from the equation

$$E_i = \sum_{j=1}^v e_{l_j} a^{il_j}, \text{ where } a \text{ is a primitive of the codeword, comprising the steps of:}$$

triangularizing a $v \times v$ Vandermonde matrix of the elements a^{il_j} to generate elements of a matrix V ;

generating a syndrome vector W of syndromes E_i , adjusted for the triangularization of matrix V ;

generating a solution to an equation of a form $Vx M=W$, where M is a vector of the error magnitudes e_{l_j} and Vx is a vector of matrix V , having a single unknown error magnitude;

substituting to create other equations of the form $Vx M=W$ having a single unknown that can be solved for a respective error magnitude.

2(Original). The method of claim 1 wherein said triangularizing step comprises the step of recursively generating vectors of V .

3(Original). The method of claim 2 wherein said recursively generating step comprises the steps of:

setting a first vector $V(1)$ of matrix V ; and

generating subsequent vectors n , $2 \leq n \leq v$, as:

$$V(n)=(V(1) + R(A(n-l))_{v-n+1})V(n-l)$$

where $A(n)$ is equal to a^{l_n} and $R(A(n))_m$ is a vector having $A(n)$ replicated m times.

4(Original). The method of claim 3 wherein said step of setting the first vector comprises setting the first vector $V(1)$ to $\{A(1) \ A(2) \ \dots \ A(v)\}$.

5(Original). The method of claim 1 wherein said step of generating a syndrome vector comprises the step of recursively generating elements of \mathbf{W} .

6(Original). The method of claim 5 wherein said step of recursively generating elements of \mathbf{W} comprises the steps of:

for each element $\mathbf{W}(n)$:

generating a vector $T(n)=R(A(n))_n * T(n-1) + T(n-1) \ll 1$, where $R(A(n))_m$ is a vector having $A(n)$ replicated m times and is $T(n-1) \ll 1$ is a previous value of T , left-shifted and right-filled with a "0";

generating a vector $U(n)=T(n-1)*\{E(n) \ E(n-1) \ \dots \ E1\}$ and
computing $\mathbf{W}(n)$ as the sum of the elements of $U(n)$.

7(Original). A method of Reed-Solomon decoding, comprising the steps of:

generating a vector of v syndromes E_i from a received codeword;

generating v error locations l_j from the received codeword,

determining error magnitudes e_{l_j} at the v error locations from the equation

$$E_i = \sum_{j=1}^v e_{l_j} a^{il_j}, \text{ where } a \text{ is a primitive of the codeword by:}$$

triangularizing a $v \times v$ Vandermonde matrix of the elements a^{il_j} to generate elements of a matrix \mathbf{V} ;

generating a syndrome vector \mathbf{W} of syndromes E_i , adjusted for the triangularization of matrix \mathbf{V} ;

generating a solution to an equation of a form $\mathbf{Vx} \mathbf{M}=\mathbf{W}$, where \mathbf{M} is a vector of the error magnitudes e_{l_j} and \mathbf{Vx} is a vector of matrix \mathbf{V} , having a single unknown error magnitude;

substituting to create other equations of the form $\mathbf{Vx} \mathbf{M}=\mathbf{W}$ having a single unknown that can be solved for a respective error magnitude..

8(Original). The method of claim 7 wherein said triangularizing step comprises the step of recursively generating vectors of \mathbf{V} .

9(Original). The method of claim 8 wherein said recursively generating step comprises the steps of:

setting a first vector $V(1)$ of matrix V ; and
generating subsequent vectors n , $2 \leq n \leq v$, as:

$$V(n) = (V(1) + R(A(n))_{v-n+1})V(n-1)$$

where $A(n)$ is equal to a^{l_n} and $R(A(n))_m$ is a vector having $A(n)$ replicated m times.

10(Original). The method of claim 9 wherein said step of setting the first vector comprises setting the first vector $V(1)$ to $\{A(1) \ A(2) \ \dots \ A(v)\}$.

11(Original). The method of claim 7 wherein said step of generating a syndrome vector comprises the step of recursively generating elements of W .

12(Original). The method of claim 7 wherein said step of recursively generating elements of W comprises the steps of:

for each element $W(n)$:

generating a vector $T(n) = R(A(n))_n * T(n-1) + T(n-1) \ll 1$, where $R(A(n))_m$ is a vector having $A(n)$ replicated m times and is $T(n-1) \ll 1$ is a previous value of T , left-shifted and right-filled with a "0";

generating a vector $U(n) = T(n-1) * \{E(n) \ E(n-1) \ \dots \ E(1)\}$ and

computing $W(n)$ as the sum of the elements of $U(n)$.

13(Original). A Reed-Solomon decoder comprising:

circuitry for generating a vector of v syndromes E_i from a received codeword;

circuitry for generating v error locations l_j from the received codeword,

circuitry for determining error magnitudes e_{l_j} at the v error locations from the equation

$$E_i = \sum_{j=1}^v e_{l_j} a^{il_j}, \text{ where } a \text{ is a primitive of the codeword by the operations of:}$$

triangularizing a $v \times v$ Vandermonde matrix of the elements a^{il_j} to generate elements of a matrix V ;

generating a syndrome vector \mathbf{W} of syndromes E_i , adjusted for the triangularization of matrix \mathbf{V} ;

generating a solution to an equation of a form $\mathbf{Vx} \mathbf{M}=\mathbf{W}$, where \mathbf{M} is a vector of the error magnitudes e_{l_j} and \mathbf{Vx} is a vector of matrix \mathbf{V} , having a single unknown error magnitude;

substituting to create other equations of the form $\mathbf{Vx} \mathbf{M}=\mathbf{W}$ having a single unknown that can be solved for a respective error magnitude.

14(Original). The Reed-Solomon decoder of claim 13 wherein said circuitry for determining error magnitudes comprises circuitry for recursively generating vectors of \mathbf{V} .

15(Original). The Reed-Solomon decoder of claim 14 wherein said circuitry for recursively generating vectors comprises circuitry for:

setting a first vector $\mathbf{V}(1)$ of matrix \mathbf{V} ; and

generating subsequent vectors n , $2 \leq n \leq v$, as:

$$\mathbf{V}(n)=(\mathbf{V}(1) + \mathbf{R}(\mathbf{A}(n-1))_{v-n+1})\mathbf{V}(n-1)$$

where $\mathbf{A}(n)$ is equal to a^n and $\mathbf{R}(\mathbf{A}(n))_m$ is a vector having $\mathbf{A}(n)$ replicated m times.

16(Original). The Reed-Solomon decoder of claim 15 wherein said circuitry for determining error magnitudes sets the first vector $\mathbf{V}(1)$ to $\{\mathbf{A}(1) \ \mathbf{A}(2) \ \dots \ \mathbf{A}(v)\}$.

17(Original). The Reed-Solomon decoder of claim 13 wherein said circuitry for determining error magnitudes generates a syndrome vector by recursively generating elements of \mathbf{W} .

18(Original). The Reed-Solomon decoder of claim 13 wherein said circuitry for generating error magnitudes recursively generates elements of \mathbf{W} by:

for each element $\mathbf{W}(n)$:

generating a vector $\mathbf{T}(n)=\mathbf{R}(\mathbf{A}(n))_n*\mathbf{T}(n-1) + \mathbf{T}(n-1)<<1$, where $\mathbf{R}(\mathbf{A}(n))_m$ is a vector having $\mathbf{A}(n)$ replicated m times and is $\mathbf{T}(n-1)<<1$ is a previous value of \mathbf{T} , left-shifted and right-filled with a “0”;

generating a vector $U(n)=T(n-1)*\{E(n) \ E(n-1) \ \dots \ E1\}$ and computing $W(n)$ as the sum of the elements of $U(n)$.